



Computational Simulation of the Impact of System Perturbation on Stabilization of the Growth of Two Political Parties

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ABSTRACT: Qualitative characterization of the perturbation of the growth of two political parties which in nature requires a strong numerical tool for its analysis. We have therefore in this study utilized a Matlab standard solver for ordinary differential equations ODE 45 to investigate the impact of system perturbation otherwise called random fluctuation on the stabilization of two interacting political parties in a developing democracy and to evaluate the qualitative characterization of interacting political parties due to 0.01, 0.10, 5.00 and 10.00 random noise system perturbation. The result indicates that as the system perturbation increases, the level of de-stabilization of the entire political system increases. This research has re-enforced the impact of de-stabilization factors such as lack of internal democracy in political parties has on the de-stabilization of political parties in a developing democracy and if avoided, will lead to a robust and growth of parties in developing democracy. © JASEM

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Addressing the challenges of de-stabilization, it is important to investigate the impact of system perturbation driving factors such as failure in election, cross carpeting by political gladiators, political instability, etc can actually affect the potential and motivation of people in the political activities and bring about a non-participatory democracy As it can see in (Huckfeldt and Kohfeld,1992).Although, we have agreed that in a deterministic sense, the parameterization of (Arvhind

,2012) steady state solution is stable. However, what is the extent of the per capital recruitment rate η_1 of party Q and the per capital recruitment rate η_2 of party R system perturbation has on the stabilization? This is a neglected aspect of modeling two interacting political parties, which remains an open research question since the activities of political parties are dynamical in nature,(Arato,2003),.

Mathematical Formulation: Following Arvind (2012), the modeling equation which is a dynamical system, is given by

$$\frac{dP}{dt} = \phi m - \eta_1 P \frac{Q}{M} - \eta_2 P \frac{R}{M} - \phi P$$

$$\frac{dQ}{dt} = \eta_1 P \frac{Q}{M} - \gamma_1 Q \frac{R}{M} - \gamma_2 R \frac{Q}{M} - \phi Q \tag{1}$$

$$\frac{dR}{dt} = \eta_2 P \frac{R}{M} + \gamma_1 Q \frac{R}{M} - \gamma_2 R \frac{Q}{M} - \phi R$$

With the conditions the initial conditions $P(0) > 0$, $Q(0) \geq 0$, $R(0) \geq 0$.

At the steady state solution $\frac{dM}{dt} = 0$

This is an extended Lotka-Volterra multi-substitution model as in (Morris and David 2003).

Method of Solution: The numerical simulation we are proposing for the solution of this complex class of problem (1) is called the Matlab Numerical simulation software. The philosophy behind this method is to know the impact of varying the level of perturbation on the solution trajectory values.

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Following (Arvind, 2012) and (Ekaka-a, 2009), we consider the following precise deterministic parameter values;

$$\eta_1 = 0.0417, \eta_2 = 0.0278, \gamma_1 = 0.0236, \gamma_2 = 0.0097,$$

The major method of analysis is based on the implementation of the MATLAB ODE 45 numerical scheme which is a Robust Runge-kutta scheme and evaluates the qualitative characterization of interacting political parties due to 0.01, 0.1, 1, 5.0 and 10.0 random noises and observes the qualitative behavior on the solution trajectories.

The full results of applying this method are presented and discussed next.

RESULTS AND DISCUSSION

It can be observed from Table 1 to Table 5 that as the system perturbation increases, the level of destabilization of the entire system increases. So, it is cleared from this novel contribution that as the independent variable t tends to infinity, the solution trajectory due to a random system perturbation

generally outweighs the solution trajectory without a random system perturbation. On the basis of this systematic analysis, we have observed that a random noise system perturbation has the potential to destabilize the deterministic dynamical system that describes the interaction between two political parties in developing democracies like Nigeria.

Table 1: Evaluating the qualitative characterization of interacting political parties due to 0.01 random noise system perturbation using ODE 45

Example	RS	$\eta_1(4)$	η_1rn	$\eta_2(4)$	η_2rn
1	1	1.43651711325650	1.0609576567136	10.7980529152492	2.48821529715523
2	2	1.43651711325650	1.05790549566056	10.7980529152492	2.48781481084994
3	3	1.43651711325650	1.06625404474447	10.7980529152492	2.49029570275644
4	4	1.43651711325650	1.05680699689741	10.7980529152492	2.48828934088830
5	5	1.43651711325650	1.05991760322433	10.7980529152492	2.48305162621826
6	6	1.43651711325650	1.06133475898536	10.7980529152492	2.48289274320012
7	7	1.43651711325650	1.06085914104013	10.7980529152492	2.48365162051966
8	8	1.43651711325650	1.06127674399038	10.7980529152492	2.48701821842759
9	9	1.43651711325650	1.05824156275381	10.7980529152492	2.48131002946453
10	10	1.43651711325650	1.05739994984151	10.7980529152492	2.48395500010629

When the value of random noise perturbation is 0.01, the numerical simulation random noise value ranges from the value of 1.05824156275381 to 1.06625404474447 and 2.48131002946453 to 2.49029570275644 for the intrinsic growth rates η_1rn and η_2rn respectively of the interacting two political parties.

Table 2: Evaluating the qualitative characterization of interacting political parties due to 0.1 random noise system perturbation using ODE 45

Example	RS	$\eta_1(4)$	η_1rn	$\eta_2(4)$	η_2rn
1	1	1.43651711325650	1.2278527712168	10.7980529152492	2.62400631245802
2	2	1.43651711325650	1.17524014827114	10.7980529152492	2.69697672824029
3	3	1.43651711325650	1.25026500565991	10.7980529152492	2.63107198302351
4	4	1.43651711325650	1.22984058004148	10.7980529152492	2.69833190689295
5	5	1.43651711325650	1.21890869254285	10.7980529152492	2.65872818385740
6	6	1.43651711325650	1.18967112729009	10.7980529152492	2.67038812676433
7	7	1.43651711325650	1.19737145125192	10.7980529152492	2.69471287056911
8	8	1.43651711325650	1.16667083134789	10.7980529152492	2.70316472749864
9	9	1.43651711325650	1.21272231323964	10.7980529152492	2.68372387701938
10	10	1.43651711325650	1.16461465308184	10.7980529152492	2.71849117110819

When the value of random noise perturbation is 0.1, the numerical simulation random noise value ranges from the value of 1.16461465308184 to 1.25026500565991 and 2.62400631245802 to 2.71849117110819 for the intrinsic growth rates η_1rn and η_2rn respectively of the interacting two political parties.

Table 3: Evaluating the qualitative characterization of interacting political parties due to 1.0 random noise system perturbation using ODE45

Example	RS	$\eta_1(4)$	η_1rn	$\eta_2(4)$	η_2rn
1	1	1.43651711325650	2.5462969084112	10.7980529152492	4.48334765667066
2	2	1.43651711325650	2.5374269585154	10.7980529152492	4.41568117876753
3	3	1.43651711325650	2.5802537978094	10.7980529152492	4.59931999407648
4	4	1.43651711325650	2.4309617589688	10.7980529152492	4.56505670388324
5	5	1.43651711325650	2.5053024168849	10.7980529152492	4.57407583642139
6	6	1.43651711325650	2.6270813291340	10.7980529152492	4.76683233496164
7	7	1.43651711325650	2.5189851694690	10.7980529152492	4.55790894565828
8	8	1.43651711325650	2.5644207874087	10.7980529152492	4.48189851234733
9	9	1.43651711325650	2.3973594428491	10.7980529152492	4.44695160895281
10	10	1.43651711325650	2.5133940503448	10.7980529152492	4.58050523700687

Similarly, when the value of random noise perturbation is 1.0, the numerical simulation

Random noise value ranges from the value of 2.3973594428491 to 2.6270813291340 and 4.41568117876753 to 4.76683233496164 for the intrinsic growth rates η_1rn and η_2rn respectively of the interacting two political parties.

Table 4: Evaluating the qualitative characterization of interacting political parties due to 5.0 random noise system perturbation using ODE45

Example	RS	$\eta_1(4)$	η_1rn	$\eta_2(4)$	η_2rn
1	1	1.43651711325650	6.3016067016574	10.7980529152492	13.3789554796706
2	2	1.43651711325650	6.378955479670	10.7980529152492	13.2439302145988
3	3	1.43651711325650	6.7633452903934	10.7980529152492	13.4420359648161
4	4	1.43651711325650	6.5814343554167	10.7980529152492	14.2039463727159
5	5	1.43651711325650	6.6064496058526	10.7980529152492	14.3230790042630
6	6	1.43651711325650	6.4026092488267	10.7980529152492	14.6951902151518
7	7	1.43651711325650	6.6843117554080	10.7980529152492	13.0967679462801
8	8	1.43651711325650	6.6336612871534	10.7980529152492	13.1949554862764
9	9	1.43651711325650	6.8926304345713	10.7980529152492	14.1384515328078
10	10	1.43651711325650	6.8509580132006	10.7980529152492	14.2899380729331

When the value of random noise perturbation is 5.0, the numerical simulation

Random noise value ranges from the value of 6.3016067016574 to 6.8926304345713 and 13.1949554862764 to 14.6951902151518 for the intrinsic growth rates η_1rn and η_2rn respectively of the interacting two political parties.

Table 5: Evaluating the qualitative characterization of interacting political parties due to 10.0 random noise system perturbation using ODE45

Example	RS	$\eta_1(4)$	η_1rn	$\eta_2(4)$	η_2rn
1	1	1.43651711325650	8.8840468198663	10.7980529152492	26.9016524675767
2	2	1.43651711325650	9.3016792483179	10.7980529152492	26.4605476780696
3	3	1.43651711325650	8.8141689814512	10.7980529152492	25.5261725024278
4	4	1.43651711325650	9.9403227931174	10.7980529152492	25.6636555375322
5	5	1.43651711325650	9.5961209073984	10.7980529152492	25.9218805979897
6	6	1.43651711325650	8.9128463048855	10.7980529152492	25.5802604455235
7	7	1.43651711325650	9.2914952824882	10.7980529152492	25.7037420305581
8	8	1.43651711325650	9.3784420158988	10.7980529152492	26.7615214099693
9	9	1.43651711325650	9.3819929912604	10.7980529152492	27.8023554675845
10	10	1.43651711325650	9.8893213894481	10.7980529152492	25.1545358969362

Lastly, when the value of random noise perturbation is 10.0, the numerical simulation

Random noise value ranges from the value of 8.8141689814512 to 9.9403227931174 and 25.1545358969362 to 27.8023554675845 for the intrinsic growth rates η_1rn and η_2rn respectively of the interacting two political parties.

From the analysis carried out, we would recommend a reduction in the factors that bring about fluctuation and cause de-stabilization. For example, lack of internal democracy, fail electoral promises, imposition of candidates, can have negative implications in the growth and survival of political parties

Conclusion: This paper has presented a novel contribution to knowledge by successfully utilizing numerical simulation technique to re-enforce the fact that a reduction in the factors that cause the de-stabilization of survival of political parties in a developing democracy, will lead to a robust and growth of parties.

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